MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL **Strand 1: Number and Operations** CONCEPT 2008 PO ITEM DESCRIPTION 2003 PO ITEM DESCRIPTION 1. Number Sense Classify real numbers as members of one or 1 Justify with examples the relation between the number system being used (natural more subsets: natural, whole, integers, rational, or irrational numbers. numbers, whole numbers, integers, rational numbers and irrational numbers) and the question of whether or not an equation has a solution in that number system. Sort sets of numbers as finite or infinite, 2 3 Distinguish between finite and infinite sets of and justify the sort. numbers. 3 *Express that the distance between two numbers is the absolute value of their difference.* MHS-**Moved to Strand 1 Concept 2** 2 Identify properties of the real number system: S1C2-02 commutative, associative, distributive, identity, inverse, and closure. Select the grade-level appropriate operation to 1 Solve word problems involving absolute 2. Numerical 1 **Operations** value, powers, roots, and scientific solve word problems. 2 Solve word problems using grade-level notation. appropriate operations and numbers. Summarize the properties of and Simplify numerical expressions including signed 2 3 connections between real number numbers and absolute values. operations; justify manipulations of 7 Simplify numerical expressions using the order of expressions using the properties of real operations. number operations. MHS-Identify properties of the real number system: S1C1-02 commutative, associative, distributive, identity, inverse, and closure. MHS-Calculate powers and roots of real numbers, both Calculate powers and roots of rational and 3 rational and irrational, using technology when irrational numbers. S3C3-14 appropriate. Compute using scientific notation. Compute using scientific notation. 4 6

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

| Strand 1: Number and Operations | | | | |
|---------------------------------|-----------------|---|---------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 2. Numerical Operations | MHS- S3C1-03 | Moved to Strand 3 Concept 1 | 4 | Apply subscripts to represent ordinal position. |
| • | MHS- S5C2-02 | Moved to Strand 5 Concept 2 | 5 | Use grade level-appropriate mathematical terminology. |
| 3. Estimation | 1 | Determine rational approximations of irrational numbers. | 3 | Determine rational approximations of irrational numbers. |
| | 2 | Use estimation to determine the reasonableness of a solution. | 2 | Determine if a solution to a problem is reasonable. |
| | 3 | *Determine when an estimate is more appropriate than an exact answer.* | | |
| | 4 | Estimate the location of the rational or irrational numbers on a number line. | 3 | Determine rational approximations of irrational numbers. |
| | M08- S1C3-01 | Moved to Grade 8 | 1 | Solve grade-level appropriate problems using estimation. |

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| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
|----------------------------------|---------|---|---------|---|
| 1. Data Analysis (Statistics) | 1 | Draw inferences about data sets from lists, tables, matrices, and plots. | 9 | Draw inferences from charts, tables, graphs, plots, or data sets. |
| | 2 | Organize collected data into an appropriate graphical representation with or without technology. | 2 | Organize collected data into an appropriate graphical representation. |
| | 3 | Display data, including paired data, as lists, tables, matrices, and plots with or | 3 | Display data as lists, tables, matrices, and plots. |
| | | without technology; make predictions and observations about patterns or departures from patterns. | 4 | Construct equivalent displays of the same data. |
| | | | 7 | Make reasonable predictions based upon linear patterns in data sets or scatter plots. |
| | | | 8 | Make reasonable predictions for a set of data, based on patterns. |
| | | | 14 | Determine whether displayed data has positive, negative, or no correlation. |
| | | | 15 | Identify a normal distribution. |
| | 4 | Make inferences by comparing data sets using one or more summary statistics. | 10 | Apply the concepts of mean, median, mode, range, and quartiles to summarize data sets. |
| | 5 | Determine which measure of center is most appropriate in a given situation and explain why. | 6 | Identify which of the measures of central tendency is most appropriate in a given situation |
| | 6 | Evaluate the reasonableness of conclusions drawn from data analysis. | 11 | Evaluate the reasonableness of conclusions drawn from data analysis. |
| | 7 | Identify misrepresentations and distortions in displays of data and explain why they are misrepresentations or distortions. | 5 | Identify graphic misrepresentations and distortions of sets of data. |
| | 8 | *Design simple experiments or investigations and collect data to answer questions.* | | |
| | | REMOVED | 1 | Formulate questions to collect data in contextual situations. |

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| Strand 2: Data Analysis, Probability, and Discrete Mathematics | | | | | |
|--|------------------|---|-----------------|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 1. Data Analysis (Statistics) | MCWR- S2C1-04 | Moved to College Work Readiness | 12 | Recognize and explain the impact of interpreting data (making inferences or drawing conclusions) from a biased sample. | |
| | MCWR- S2C1-08 | Moved to College Work Readiness | 13 | Draw a line of best fit for a scatter plot. | |
| | | REMOVED | 16 | Identify differences between sampling and census. | |
| | M08- S2C1-04 | Moved to Grade 8 | 17 | Identify differences between biased and unbiased samples. | |
| 2. Probability | 1 | Make predictions and solve problems based on theoretical probability models. | 1 | Find the probability that a specific event will occur, with or without replacement. | |
| | | | 3 | Predict the outcome of a grade-level appropriate probability experiment. | |
| | 2 | Determine the theoretical probability of events, estimate probabilities using | 4 | Record the data from performing a grade-level appropriate probability experiment. | |
| | | experiments, and compare the two. | 5 | Compare the outcome of an experiment to predictions made prior to performing the experiment. | |
| | | | 7 | Compare the results of two repetitions of the same grade-level appropriate probability experiment. | |
| | | | MHS- S1C3-01 | Solve grade-level appropriate problems using estimation. | |
| | 3 | Use simulations to model situations involving independent and dependent events. | 6 | Distinguish between independent and dependent events. | |
| | 4 | *Explain and use the law of large numbers (that experimental results tend to approach theoretical probabilities after a large number of trials).* | | | |
| | 5 | Use concepts and formulas of area to calculate geometric probabilities. | 2 | Determine simple probabilities related to geometric figures. | |

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| | Strand 2: Data Analysis, Probability, and Discrete Mathematics | | | |
|--|--|---|---------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 3. Systematic Listing and Counting | 1 | *Apply the addition and multiplication principles of counting, representing these principles algebraically using factorial notation.* | | |
| | 2 | Apply appropriate means of computing the number of possible arrangements of items using permutations where order matters, and combinations where order does not matter. | 2 | Determine when to use combinations versus permutations in counting objects. |
| | | | 3 | Use combinations or permutations to solve contextual problems. |
| | 3 | Determine the number of possible outcomes of an event. | 1 | Determine the number of possible outcomes for a contextual event using a chart, a tree diagram, or the counting principle. |
| 4. Vertex-Edge Graphs | 1 | *Solve network problems using graphs and matrices.* | | |

| Strand 3: Patterns, Algebra, and Functions | | | | |
|--|---------|--|-----------------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Patterns | 1 | Recognize, describe, and analyze sequences using tables, graphs, words, or symbols; use sequences in modeling. | 1 | Communicate a grade-level appropriate iterative or recursive pattern, using symbols or numbers. |
| | 2 | Determine a specific term of a sequence. | 2 | Find the <i>n</i> th term of an iterative or recursive pattern. |
| | 3 | Create sequences using explicit and recursive formulas involving both | 3 | Evaluate problems using basic recursion formulas. |
| | | subscripts and function notation. | MHS- S1C2-04 | Apply subscripts to represent ordinal position. |

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| | Strand 3: Patterns, Algebra, and Functions | | | | |
|--------------------------------|--|---|-----------------|---|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 2. Functions and Relationships | 1 | Sketch and interpret a graph that models a given context, make connections | 2 | Describe a contextual situation that is depicted by a given graph. | |
| | | between the graph and the context, and solve maximum and minimum problems | 3 | Identify a graph that models a given real-world situation. | |
| | | using the graph. | 4 | Sketch a graph that models a given contextual situation. | |
| | | | 6 | Determine the solution to a contextual maximum/minimum problem, given the graphical representation. | |
| | 2 | Determine if a relationship represented by an equation, graph, table, description, or set of ordered pairs is a function. | 1 | Determine if a relationship is a function, given a graph, table, or set of ordered pairs. | |
| | 3 | Use function notation; evaluate a function at a specified value in its domain. | MHS- S3C3-01 | Evaluate algebraic expressions, including absolute value and square roots. | |
| | 4 | Use equations, graphs, tables, descriptions, or sets of ordered pairs to | 7 | Express the relationship between two variables using tables/matrices, equations, or graphs. | |
| | | express a relationship between two variables. | 8 | Interpret the relationship between data suggested by tables/matrices, equations, or graphs. | |
| | | | MHS- S3C3-05 | Translate a sentence written in context into an algebraic equation involving multiple operations. | |
| | | | MHS- S3C3-07 | Write a linear algebraic sentence that represents a data set that models a contextual situation. | |
| | 5 | Recognize and solve problems that can be modeled using a system of two equations in two variables. | MHS- S3C3-12 | Solve systems of linear equations in two variables (integral coefficients and rational solutions). | |
| | 6 | Recognize and solve problems that can be modeled using a quadratic function. | MHS- S3C3-17 | Solve quadratic equations. | |

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| | Strand 3: Patterns, Algebra, and Functions | | | | |
|--------------------------------|--|---|-----------------|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 2. Functions and Relationships | 7 | Determine domain and range of a function from an equation, graph, table, description, or set of ordered pairs. | 5 | Determine domain and range for a function. | |
| | MHS- S3C3-04 | Moved to Strand 3 Concept 3 | 9 | Determine from two linear equations whether the lines are parallel, perpendicular, coincident, or intersecting but not perpendicular. | |
| 3. Algebraic Representations | 1 | Create and explain the need for equivalent forms of an equation or expression. | 5 | Translate a written expression or sentence into a mathematical expression or sentence. Translate a sentence written in context into an | |
| | | expression. | 5 | algebraic equation involving multiple operations. | |
| | 2 | Solve formulas for specified variables. | MHS- S3C4-02 | Solve formulas for specified variables. | |
| | 3 | Write an equation given a table of values, | 6 | Write a linear equation for a table of values. | |
| | | two points on the line, the slope and a point on the line, or the graph of the line. | 10 | Write an equation of the line given: two points on the line, the slope and a point on the line, or the graph of the line. | |
| | 4 | Determine from two linear equations whether the lines are parallel, perpendicular, coincident, or intersecting but not perpendicular. | MHS- S3C2-09 | Determine from two linear equations whether the lines are parallel, perpendicular, coincident, or intersecting but not perpendicular. | |
| | 5 | Solve linear equations and equations involving absolute value, with one | 8 | Solve linear (first degree) equations in one variable (may include absolute value). | |
| | | variable. | 11 | Solve an algebraic proportion. | |
| | 6 | Solve linear inequalities in one variable. | 9 | Solve linear inequalities in one variable. | |
| | 7 | Solve systems of two linear equations in two variables. | 12 | Solve systems of linear equations in two variables (integral coefficients and rational solutions). | |
| | 8 | Simplify and evaluate polynomials, | 2 | Simplify algebraic expressions. | |
| | | rational expressions, expressions containing absolute value, and radicals. | 15 | Simplify square roots and cube roots with monomial radicands (including those with variables) that are perfect squares or perfect cubes. | |

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| | Strand 3: Patterns, Algebra, and Functions | | | | |
|---------------------------------|--|--|---------|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 3. Algebraic Representations | 9 | Multiply and divide monomial expressions with integer exponents. | 3 | Multiply and divide monomial expressions with integral exponents. | |
| | 10 | *Add, subtract, and multiply polynomial and rational expressions.* | | | |
| | 11 | Solve square root equations involving only one radical. | 16 | Solve square root radical equations involving only one radical. | |
| | 12 | *Factor quadratic polynomials in the form of $ax^2 + bx + c$ where a , b , and c are integers.* | | | |
| | 13 | Solve quadratic equations. | 11 | Solve an algebraic proportion. | |
| | | | 17 | Solve quadratic equations. | |
| | 14 | *Factor higher order polynomials.* | | | |
| | 15 | Solve problems using operations with matrices. | 13 | Add, subtract, and perform scalar multiplication with matrices. | |
| | MHS- S3C2-03 | Moved to Strand 3 Concept 2 | 1 | Evaluate algebraic expressions, including absolute value and square roots. | |
| | MHS- S3C2-04 | Moved to Strand 3 Concept 2 | 7 | Write a linear algebraic sentence that represents a data set that models a contextual situation. | |
| | MHS- S1C2-03 | Moved to Strand 1 Concept 2 | 14 | Calculate powers and roots of real numbers, both rational and irrational, using technology when appropriate. | |
| | MHS- S4C1-11 | Moved to Strand 4 Concept 1 | 18 | Identify the sine, cosine, and tangent ratios of the acute angles of a right triangle. | |
| 4. Analysis of Change | 1 | Determine the slope and intercepts of the graph of a linear function, interpreting slope as a constant rate of change. | 1 | Determine slope, x-, and y-intercepts of a linear equation. | |
| | 2 | *Solve problems involving rate of change.* | | | |
| | 3 | *Solve interest problems.* | | | |
| | MHS- S3C3-02 | Moved to Strand 3 Concept 3 | 2 | Solve formulas for specified variables. | |

^{*} This performance objective is new to the 2008 Mathematics Standard Articulated by Grade Level.

| | | Strand 4: Geometry and M | easuremen | t |
|-------------------------|---------|--|-----------------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 1. Geometric Properties | 1 | Use the basic properties of a circle (relationships between angles, radii, | 7 | Solve problems by applying the relationship between circles, angles, and intercepted arcs. |
| | | intercepted arcs, chords, tangents, and secants) to prove basic theorems and solve problems. | 8 | Solve problems by applying the relationship between radii, diameters, chords, tangents, or secants. |
| | 2 | Visualize solids and surfaces in 3- | 3 | Make a net to represent a 3-dimensional object. |
| | | dimensional space when given 2- | 4 | Make a 3-dimensional model from a net. |
| | | dimensional representations and create 2-dimensional representations for the surfaces of 3-dimensional objects. | 5 | Draw 2-dimensional and 3-dimensional figures with appropriate labels. |
| | 3 | Create and analyze inductive and deductive arguments concerning geometric ideas and relationships. | MHS- S5C2-07 | Create inductive and deductive arguments concerning geometric ideas and relationships, such as congruence, similarity, and the Pythagorean relationship. |
| | | | MHS- S5C2-08 | Critique inductive and deductive arguments concerning geometric ideas and relationships, such as congruence, similarity, and the Pythagorean relationship. |
| | 4 | *Apply properties, theorems, and constructions about parallel lines, perpendicular lines, and angles to prove theorems.* | | |
| | 5 | *Explore Euclid's five postulates in the plane and their limitations.* | | |
| | 6 | Solve problems using angle and side length relationships and attributes of | 1 | Identify the attributes of special triangles (isosceles, equilateral, right). |
| | | polygons. | 6 | Solve problems related to complementary, supplementary, or congruent angle concepts. |
| | | | 14 | Solve contextual situations using angle and side length relationships. |
| | | | M08- S4C4-05 | Find the measure of a missing interior angle in a triangle or quadrilateral. |

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| | Strand 4: Geometry and Measurement | | | | |
|-----------------------------|------------------------------------|---|-----------------|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 1. Geometric Properties | 7 | Use the hierarchy of quadrilaterals in deductive reasoning. | 2 | Identify the hierarchy of quadrilaterals. | |
| | 8 | Prove similarity and congruence of triangles. | 11 | Determine when triangles are congruent by applying SSS, ASA, AAS, or SAS. | |
| | | | 12 | Determine when triangles are similar by applying SAS, SSS, or AA similarity postulates. | |
| | 9 | Solve problems using the triangle inequality property. | 9 | Solve problems using the triangle inequality property. | |
| | | | M07- S4C1-09 | Model the triangle inequality theorem using manipulatives. | |
| | | | M08- S4C1-09 | Determine whether three given lengths can form a triangle. | |
| | 10 | Solve problems using right triangles, including special triangles. | 10 | Solve problems using special case right triangles. | |
| | 11 | Solve problems using the sine, cosine, and tangent ratios of the acute angles of a right triangle. | MHS- S3C3-18 | Identify the sine, cosine, and tangent ratios of the acute angles of a right triangle. | |
| | M05- S4C1-01 | Moved to Grade 5 | 13 | Construct a triangle congruent to a given triangle. | |
| 2. Transformation of Shapes | 1 | Determine whether a transformation of a 2-dimensional figure on a coordinate plane represents a translation, reflection, rotation, or dilation and whether congruence is preserved. | 4 | Determine whether a given pair of figures on a coordinate plane represents a translation, reflection, rotation, or dilation. | |
| | 2 | Determine the new coordinates of a point when a single transformation is performed on a 2-dimensional figure. | 3 | Determine the new coordinates of a point when a single transformation is performed on a planar geometric figure. | |
| | 3 | Sketch and describe the properties of a 2-dimensional figure that is the result of | 1 | Sketch the planar figure that is the result of two or more transformations. | |
| | | two or more transformations. | 2 | Identify the properties of the planar figure that is the result of two or more transformations. | |
| | | | 5 | Classify transformations based on whether they produce congruent or similar figures. | |

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| Strand 4: Geometry and Measurement | | | | |
|------------------------------------|---------|--|-----------------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 2. Transformation of Shapes | 4 | Determine the effects of a single transformation on linear or area measurements of a 2-dimensional figure. | 6 | Determine the effects of a single transformation on linear or area measurements of a planar geometric figure. |
| 3. Coordinate Geometry | 1 | Determine how to find the midpoint between two points in the coordinate plane. | 5 | Determine the midpoint between two points in a coordinate system. |
| | 2 | *Illustrate the connection between the distance formula and the Pythagorean Theorem.* | | |
| | 3 | Determine the distance between two points in the coordinate plane. | 7 | Determine the distance between two points in the coordinate system. |
| | 4 | Verify characteristics of a given geometric figure using coordinate formulas for distance, midpoint, and slope to confirm parallelism, perpendicularity, and congruence. | MHS- S5C2-14 | Verify characteristics of a given geometric figure using coordinate formulas such as distance, midpoint, and slope to confirm parallelism, perpendicularity, and congruency. |
| | 5 | Graph a linear equation or linear | 2 | Graph a linear equation in two variables. |
| | | inequality in two variables. | 3 | Graph a linear inequality in two variables. |
| | 6 | Describe how changing the parameters of a linear function affect the shape and position of its graph. | 6 | Determine changes in the graph of a linear function when constants and coefficients in its equation are varied. |
| | 7 | Determine the solution to a system of linear equations in two variables from the graphs of the equations. | 4 | Determine the solution to a system of equations in two variables from a given graph. |
| | 8 | Graph a quadratic function and interpret x-intercepts as zeros. | 1 | Graph a quadratic equation with lead coefficient equal to one. |
| 4. Measurement | 1 | Use dimensional analysis to keep track of units of measure when converting. | M07- S4C4-03 | Converts measurement from U.S. Customary to metric, and vice versa. |
| | 2 | Find the length of a circular arc; find the | 5 | Find the length of a circular arc. |
| | | area of a sector of a circle. | 6 | Find the area of a sector of a circle. |
| | 3 | Determine the effect that changing dimensions has on the perimeter, area, or volume of a figure. | 4 | Compare perimeter, area, or volume of figures when dimensions are changed. |

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| Strand 4: Geometry and Measurement | | | | |
|------------------------------------|-----------------|--|---------|---|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 4. Measurement | 4 | Solve problems involving similar figures using ratios and proportions. | 9 | Solve scale factor problems using ratios and proportions. |
| | | | 10 | Solve applied problems using similar triangles. |
| | 5 | Calculate the surface area and volume of 3-dimensional figures and solve for | 2 | Calculate the volumes of 3-dimensional geometric figures. |
| | | missing measures. | 3 | Calculate the surface areas of 3-dimensional geometric figures. |
| | | | 7 | Solve for missing measures in a pyramid (i.e., slant height, height). |
| | M07- S4C1-04 | Moved to Grade 7 | 8 | Find the sum of the interior and exterior angles of a polygon. |
| | | REMOVED - exterior angles | 8 | Find the sum of the interior and exterior angles of a polygon. |
| | M07- S4C4-03 | Moved to Grade 7 | 1 | Calculate the area of geometric shapes composed of two or more geometric figures. |

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| Strand 5: Structure and Logic | | | | | | | |
|--|---------|---|------------------------------------|---|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | | |
| 1. Algorithms and Algorithmic | 1 | Select an algorithm that explains a particular mathematical process; | 4 | Select an algorithm that explains a particular mathematical process. | | | |
| Thinking | | determine the purpose of a simple mathematical algorithm. | 5 | Determine the purpose of a simple mathematical algorithm. | | | |
| | 2 | Analyze algorithms for validity and equivalence recognizing the purpose of the algorithm. | 1 | Determine whether a given procedure for simplifying an expression is valid. | | | |
| | | | 2 | Determine whether a given procedure for solving an equation is valid. | | | |
| | | | 3 | Determine whether a given procedure for solving a linear inequality is valid. | | | |
| | | | 6 | Determine whether given simple mathematical algorithms are equivalent. | | | |
| 2. Logic, Reasoning, Problem Solving, and Proof | 1 | *Analyze a problem situation, determine the question(s) to be answered, organize given information, determine how to represent the problem, and identify implicit and explicit assumptions that have been made.* | | | | | |
| | 2 | Solve problems by formulating one or more strategies, applying the strategies, verifying the solution(s), and communicating the reasoning used to obtain the solution(s). | MHS- S1C2-01 | Select the grade-level appropriate operation to solve word problems. | | | |
| | | | MHS- S1C2-02 MHS- S1C2-05 | Solve word problems using grade-level appropriate operations and numbers. Use grade level-appropriate mathematical terminology. | | | |
| | 3 | Evaluate a solution for reasonableness and interpret the meaning of the solution in the context of the original problem. | 6 | Analyze assertions related to a contextual situation by using principles of logic. Distinguish valid arguments from invalid arguments. | | | |

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| Strand 5: Structure and Logic | | | | | | |
|---|---------|---|---------|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 2. Logic, Reasoning, Problem Solving, and Proof | 4 | *Generalize a solution strategy for a single problem to a class of related problems; explain the role of generalizations in inductive and deductive reasoning.* | | | | |
| | 5 | Summarize and communicate mathematical ideas using formal and informal reasoning. | 7 | Create inductive and deductive arguments concerning geometric ideas and relationships, such as congruence, similarity, and the Pythagorean relationship. | | |
| | 6 | Synthesize mathematical information from multiple sources to draw a conclusion, make inferences based on mathematical information, evaluate the conclusions of others, analyze a mathematical argument, and recognize flaws or gaps in reasoning. | 8 | Critique inductive and deductive arguments concerning geometric ideas and relationships, such as congruence, similarity, and the Pythagorean relationship. | | |
| | 7 | *Find structural similarities within different algebraic expressions and geometric figures.* | | | | |
| | 8 | Use inductive reasoning to make conjectures, use deductive reasoning to | 3 | Write an appropriate conjecture given a certain set of circumstances. | | |
| | | analyze and prove a valid conjecture, and develop a counterexample to refute an | 5 | Identify a valid conjecture using inductive reasoning. | | |
| | | invalid conjecture. | 9 | Identify a counterexample for a given conjecture. | | |
| | | | 10 | Construct a counterexample to show that a given conjecture is false. | | |
| | 9 | State the inverse, converse, and contrapositive of a given statement and | 11 | State the inverse, converse, or contrapositive of a given statement. | | |
| | | state the relationship between the truth value of these statements and the original statement. | 12 | Determine if the inverse, converse, or contrapositive of a given statement is true or false. | | |

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| Strand 5: Structure and Logic | | | | | | | |
|--|-----------------|--|---------|---|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | | |
| 2. Logic, Reasoning, Problem Solving, and Proof | 10 | List related <i>if then</i> statements in logical order. | 2 | List related if then statements in logical order. | | | |
| | 11 | Draw a simple valid conclusion from a given ifthen statement and a minor premise. | 1 | Draw a simple valid conclusion from a given ifthen statement and a minor premise. | | | |
| | 12 | Construct a simple formal deductive proof. | 13 | Construct a simple formal or informal deductive proof. | | | |
| | 13 | *Identify and explain the roles played by definitions, postulates, propositions and theorems in the logical structure of mathematics, including Euclidean geometry.* | | | | | |
| | MHS- S4C3-04 | Moved to Strand 4 Concept 3 | 14 | Verify characteristics of a given geometric figure using coordinate formulas such as distance, mid-point, and slope to confirm parallelism, perpendicularity, and congruency. | | | |

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